Discovery and Characterization of Transiting Super Earths Using an All-Sky Transit Survey and Follow-up by the *James Webb Space Telescope*

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ABSTRACT. Doppler and transit surveys are finding extrasolar planets of ever smaller mass and radius, and are now sampling the domain of super Earths $(1-3R_{\oplus})$. Recent results from the Doppler surveys suggest that discovery of a transiting super Earth in the habitable zone of a lower main sequence star may be possible. We evaluate the prospects for an all-sky transit survey targeted to the brightest stars, that would find the most favorable cases for photometric and spectroscopic characterization using the James Webb Space Telescope (JWST). We use the proposed Transiting Exoplanet Survey Satellite (TESS) as representative of an all-sky survey. We couple the simulated TESS yield to a sensitivity model for the MIRI and NIRSpec instruments on JWST. Our sensitivity model includes all currently known and anticipated sources of random and systematic error for these instruments. We focus on the TESS planets with radii between those of Earth and Neptune. Our simulations consider secondary eclipse filter photometry using JWST/MIRI, comparing the 11 and 15 μ m bands to measure CO₂ absorption in super Earths, as well as JWST/NIRSpec spectroscopy of water absorption from 1.7–3.0 μ m, and CO₂ absorption at 4.3 μ m. We find that JWST will be capable of characterizing dozens of TESS super Earths with temperatures above the habitable range, using both MIRI and NIRspec. We project that TESS will discover about eight nearby habitable transiting super Earths, all orbiting lower-main-sequence stars. The principal sources of uncertainty in the prospective JWST characterization of habitable super Earths are super-Earth frequency and the nature of super-Earth atmospheres. Based on our estimates of these uncertainties, we project that JWST will be able to measure the temperature and identify molecular absorptions (water, CO₂) in one to four nearby habitable TESS super Earths orbiting lower-main-sequence stars.

1. INTRODUCTION

In the quest to measure the spectrum of a habitable exoplanet, the observer must successfully disentangle the planetary flux from that of the central star. Two methods are currently in use for the direct study of gas-giant exoplanets, and practitioners of each are working to apply these methods to the study of rocky exoplanets. In the first technique, the planet and star are

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separated spatially through high angular resolution imaging (Kalas et al. 2008; Marois et al. 2008). This method favors systems wherein the angular separation is as large as possible. The second method obviates the need for high angular resolution imaging by studying the combined light of the planet and star in transiting systems. In these systems, the planet and star undergo periodic mutual eclipses (see Charbonneau et al. 2007 for a review), and the emission from each is subsequently separated with the knowledge of the previously characterized orbit. The primary disadvantage of the latter approach is obvious: only a small fraction of exoplanets will have their orbits aligned so as to undergo eclipses as viewed from the Earth.

The transit method offers several advantages that motivate its further study. The first is that of technological simplicity, since it does not require the development of extreme contrast ratio direct imaging. The second is that of scientific impact: eclipsing systems, for which the photometric transit and stellar radial velocity orbit have been observed, permit a geometric determination of the planetary radius and a dynamical estimate of the planetary mass by a means that is virtually free of astrophysical assumption. For such systems, the interpretation of the hemisphereaveraged spectrum is likely to be more scientifically fruitful than for systems lacking direct measurements of the masses

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or radii. For example, without a knowledge of the planet radius, there exists a degeneracy between the emitting area and surface flux (see, e.g., Kalas et al. 2008). More generally, the bulk composition and physical structures of transiting exoplanets are likely to be well constrained, and inferences about the atmosphere (for example, its chemical composition) are likely to be far more penetrating than for cases in which only the spectrum is available.

Over the past seven years, the characterization of the atmospheres of Gyr-old planets orbiting solar peers has proceeded rapidly and exclusively through the study of combined light of the planet and star in transiting systems. A partial list of such successful studies includes Charbonneau et al. (2002, 2005, 2008), Deming et al. (2005, 2006, 2007), Grillmair et al. (2007, 2008), Harrington et al. (2006, 2007), Knutson et al. (2007, 2008, 2009), Richardson et al. (2007), Swain et al. (2008, 2009), Tinetti et al. (2007), and Vidal-Madjar et al. (2003). All of the detections listed in the previous sentence were accomplished with either the *Hubble Space Telescope (HST)* or *Spitzer Space Telescope*, two general purpose, space-based facilities, neither of which was optimized for exoplanet studies (indeed, these studies were not anticipated during the development of either facility).

Since there is currently intense interest in rocky super-Earth exoplanets,¹⁰ it is desirable to explore the factors that will limit their discovery and study using transit/eclipse methodology. We consider the coming James Webb Space Telescope (JWST) and ask what it could accomplish for studies of the atmospheres of transiting exoplanets, especially for smaller, rocky, and potentially habitable worlds. We note that neither HST nor Spitzer served as the discovery observatory for the planets they characterized: rather, the tasks of discovery and characterization were split, with ground-based surveys pursuing the former and these two spacecraft conducting the latter. Similarly, we anticipate that JWST will be able to undertake characterization studies of the atmospheres of habitable worlds, but only if these objects are identified in nearby, transiting systems by a separate discovery effort. Since the most favorable systems are the closest ones, and very high photometric precision is needed for long time periods, a bright star, all-sky, space-borne survey such as the proposed Transiting Exoplanet Survey Satellite (TESS) is the natural starting point for our study.

The specific purpose of this article is to evaluate the potential for discovery and characterization of exoplanets by using an allsky transit survey and *JWST* follow-up. Our simulation includes planets ranging in size from Earth to Jupiter. *JWST* follow-up of Jupiter-size transiting planets would be of enormous scientific utility. Nevertheless, we here focus on planets of Neptune-size and smaller. Our analysis includes "hot super Earths" as well as those in the habitable zone $(HZ)^{11}$. We evaluate whether the sources of uncertainty for super-Earth discovery and characterization are primarily astrophysical (e.g., occurrence rate for super Earths), or technological (sensitivity of instrumentation and surveys). Our evaluation begins by projecting the yield of TESS. Although TESS is still at the proposal stage, it provides the most well-studied basis from which to project the yield of a space-borne, bright star, all-sky, transit survey. We couple the TESS planets to sensitivity calculations for specific observing modes of the Near-Infrared Spectrograph (NIRSpec) and Mid-Infrared Instrument (MIRI) instruments on *JWST*. Our intent is *not* to define and compare the relative merits of all potential modes of *JWST* exoplanet observations. Instead, we concentrate on the likely success for exoplanet characterization using two of the most obvious observational modes.

Potential *JWST* exoplanet transit observations have been discussed by several authors (Clampin et al. 2009; Greene et al. 2007; Kaltenegger & Traub 2009; Lunine et al. 2008; Seager et al. 2008; Valenti et al. 2005, 2006, 2008). Our treatment here goes beyond previous work in that we specifically include simulations of an all-sky survey, coupled to a characterization simulation that includes the *JWST*'s pointing constraints (field of regard), and anticipated *JWST* instrument- and detector-related systematic errors, based on experience with *Spitzer* and current engineering data from the *JWST* instruments.

Section 2 presents an estimate of the likely distance to the closest transiting habitable exoplanet, and § 3 describes our statistical model for the yield of TESS. Section 4 discusses a simple model for exoplanet characterization using transits and eclipses, and later sections develop more exhaustive simulations of *JWST* characterization of TESS planets: Section 5 gives our sensitivity and noise models for the *JWST* instruments, and § 6 applies these noise models to the TESS planets. Section 7 gives our conclusions and comparisons to other work.

2. THE CLOSEST TRANSITING HABITABLE EXOPLANET

It is of interest to consider the probable distance of the closest habitable planet that transits, assuming that we discover *all* nearby transiting planet systems. The probability of a transiting habitable planet within distance d can be calculated from the space density of nearby stars, if we know the distribution of planets versus orbital size for each stellar spectral type. Because these distributions are not securely known, we adopt a very general assumption. We assume that a fraction f of stars host exactly one planet in their HZ, and we place half of them at the inner HZ boundary, and half at the outer HZ boundary.

The probability of at least one transiting planet within a sphere of radius d centered on the Sun equals $1 - \prod_i p_i$, where

 $^{^{10}}$ We define a super Earth to be a rocky or icy planet having a radius less than $3R_\oplus.$

¹¹ We use the term habitable to be synonymous with a thermal equilibrium temperature range of 273–373 K, with no other requirements.



FIG. 1.—Probability of a habitable transiting planet lying within a sphere of a given distance (radius) centered on the Sun, for planet frequencies of (left to right) 1.0, 0.3, and 0.1 star^{-1} , adopting the condition that all planets lie within the HZ (see text).

 p_i is the probability that *no* planet transits star *i*, and *i* indexes the stars within distance d. Given the above assumptions on the orbital radii of the planets, and the transit probability for each planet (R_{star}/a) , this is a straightforward calculation. We adopt circular orbits, and the stellar space densities versus spectral type described in § 3. The results are shown in Figure 1 for planet frequencies of f = 1.0, 0.3, and 0.1. This calculation shows that if every star hosts a planet in the HZ, then the closest transiting habitable planet is likely (i.e., probability 0.5) to be found at d = 5 pc. This distance increases to d = 7 and 10 pc for f = 0.3 and 0.1. Moreover, even for a HZ frequency as low as f = 0.01 star⁻¹, the probable distance for the nearest example (not illustrated) is d = 22 pc. These calculations suggest good prospects for JWST characterization even if HZ planets are moderately scarce. However, there remains the practical problem of whether a given transit survey such as TESS can necessarily find the nearest examples.

3. YIELD OF AN ALL-SKY TRANSIT SURVEY

We here simulate the yield of an all-sky survey targeted primarily to bright (V < 13.5) stars, and we elaborate on how the super-Earth yield of such a survey depends on super-Earth occurrence and orbital distribution properties. We use the TESS survey (Ricker et al. 2008) as a practical example of an allsky bright star survey capable of detecting transiting super Earths. TESS is proposed to view the sky from near-Earth equatorial orbit, using an array of 6 wide-field $(18 \times 18 \text{ degree})$ refractive CCD cameras on a single spacecraft. TESS monitors 2.5×10^6 bright (V < 13.5) stars, with special attention to lower-main-sequence stars. During each orbit, TESS will monitor a 72° strip of right ascension, using several pointings. Each star in the TESS catalog will be monitored for at least 72 days. Since TESS requires two transits to identify a planet, it is insensitive to orbital periods exceeding 72 days.

3.1. Making Transiting Planets

Our Monte Carlo model of the planets to be found by TESS considers main-sequence host stars from spectral types F5 through M9. We adopt the absolute visual magnitude versus spectral type relation from Henry et al. (1994), and the main-sequence luminosity function from Reid & Hawley (2000). We convert spectral type to $T_{\rm eff}$, stellar mass and radius, using Table 4.1 of Reid & Hawley (2000).

We make planets by first generating a set of Monte Carlo stars in a cubical volume of 2000^3 pc³ centered on the Sun. This cube is larger than the TESS search space and it contains all planets that TESS will find. We assign galactic coordinates (X, Y, Z) to each star by placing them randomly within this cube, constrained by their space densities at Z = 0 versus spectral type, and enforcing an exponential distribution in height above the galactic plane (z), with 200 pc scale height. Since transiting planets require mass measurements via high-precision radial velocities, we eliminate the visually faintest stars (having V > 13.5), but we keep all stars at distances closer than 35 pc (Charbonneau & Deming 2007), regardless of their visual magnitude. Planet-hosting M dwarfs can lie at close distances and still be visually faint, because their spectral energy distribution peaks in the IR. We reason that super Earths transiting nearby M dwarfs will be so important that their radial velocities will be measured by some means, regardless of their visual magnitude. For example, IR spectroscopy could be used when it is sufficiently developed to achieve the precision needed for super Earths (Blake et al. 2007).

We assign exactly one planet to each star. We use various simple distribution formulae for orbital size and planetary radius, because the actual distributions are poorly known. An important rationale for our work is to define the expected yield of super Earths under various orbital size distributions. Our default distribution in orbital size uses a uniform probability density in log(a'), where $a' = a(L_{\odot}/L_{*})^{1/2}$, between 0 and -1.3 in log(a'). One rationale for the stellar luminosity scaling factor is that it produces a more compact planet distribution orbiting low-mass stars, consistent with evidence for close-in planet formation in some M dwarf planetary systems (Forbrich et al. 2008). Also, this scaling puts the same number of planets in each temperature zone, and is a natural way to cast the problem when interested in the HZ. At the opposite extreme, we also explore the effect of a distribution whose probability density for orbital size is uniform in a.

Because the magnitude of the transit signal depends on the radius of the planet, we use radius as the independent variable in our planet distributions. We distribute planet radii (R_p) with a uniform probability density in $\log(R_p/R_{\oplus})$, between limits of 0 and 1.1 in the log (these limits correspond to Earth and Jupitersized planets, respectively). Surface gravity is needed for subsequent simulations (§§ 5 and 6). To that end, we calculate the mass from the radius by assigning a bulk composition, and inverting the mass-radius relations of Seager et al. (2007). When $R > 2R_{\oplus}$, we use an icy bulk composition (ocean planets), and when $R > 3R_{\oplus}$ we add a H-He envelope having a depth of $1R_{\oplus}$. Planets having radii $R_p < 2R_{\oplus}$ are assigned bulk compositions of either Earth-like (silicate), or Mercury-like, with equal probability. Using this radius distribution, approximately 40% of the simulated planets are super Earths (defined by TESS as having $R \leq 3R_{\oplus}$).

For each planet, we calculate whether it transits based on random selection in proportion to the transit probability. Transit probability is the ratio of the stellar radius to the planet's orbital radius, and we used circular orbits for all planets. Using circular orbits is conservative, because transit probability increases for eccentric orbits (Barnes 2007). We also assign a random impact parameter to each transit, uniformly distributed between zero and unity. From the impact parameter, we calculate the duration of each planet's transit. Finally, we calculate the temperature of each planet, based on its orbit radius and stellar luminosity, scaling from a 287 K value at 1 AU with solar luminosity.

3.2. Finding Transiting Planets

In deciding whether TESS will discover a particular transiting planet, we take the duty cycle and sensitivity of the mission into account. TESS will observe a given location in the sky once per 96 minutes, for 72 days. For each transiting planet, we calculate the in-transit times from the planet's orbital period, assigning a random phase. We then tabulate the number of transits that overlap the TESS observing cadence, using a 10 minute time resolution. Those planets seen by TESS during at least two transits are counted as detected, providing they meet the signal-to-noise ratio (S/N) requirement.

To calculate the observed S/N of each transit, we used Phoenix model atmospheres (Hauschildt et al. 1999) for stars of each spectral type, and derived the flux incident at the TESS telescopes. The flux into the 84.6 cm² effective collecting area of the TESS telescopes (including optics throughput and detector quantum efficiency) was integrated over the 600–1000 nm bandpass of the TESS detectors, to establish a count rate for each transiting system. Given the duration of the transit, we calculate the photon-limited S/N for the aggregate of the phased transits, and we require S/N for the transit depth to be at least 7. We also eliminate planets having transit depths less than TESS's estimated systematic noise floor (100 ppm).

It is of interest to determine whether a mission in near-Earth orbit like TESS has an adequate sampling cadence to find transits, or whether it misses many. In our simulation, only a very small fraction of planets ($\ll 0.1\%$) exhibiting more than two transits within the 72 day TESS observing period were missed because of sampling. Those few cases include grazing transits of short-period planets orbiting small stars, where the transit duration was brief (typically 30 minutes). With short transit durations, a small fraction can be resonantly out of phase with the TESS 96 minute sampling interval, but the number of such cases is negligible.

We used these simulation procedures to produce a Monte Carlo realization of the TESS yield, adopting a frequency of one planet star⁻¹. The real planet frequency will differ from unity, but our results are linearly scalable to other values.

3.3. Distribution of Planets and Implications

Figure 2 shows the number of planets that TESS should find, versus their radii (R_p) , under two different assumptions concerning their orbital sizes. Using our default distribution of orbit sizes, scaling with a' (see § 3.1), TESS finds 16,244 planets. The radii of the detected planets peak just above the exoNeptune regime, at $6R_{\oplus}$. We believe that our default distribution for a is a resonable estimate. But using a distribution of orbital size that is uniform in a, the number of detected planets drops to 6845, a factor of 2.4 less. The decrease is relatively independent of planet radius, and occurs because a uniform distribution in a overweights larger orbital sizes compared to a uniform



FIG. 2.—Number of planets detected by TESS in our simulations vs. radius, using two different distributions of planet orbital distance. The solid line is our default distribution, that places planets with uniform probability in log *a*, scaled by the stellar luminosity (see text). The *dashed line* places planets with uniform probability in *a*, between 0.05 and 1.0 AU.

distribution in $\log a'$. Larger orbital sizes translate to smaller transit probabilities, and thus the yield of the survey is reduced.

The total number of small planets detected is greatly affected by the photometric sensitivity of the survey. Our default radius distribution has uniform probability density in the logarithm of R_p , and that distribution (not illustrated) slopes downward on Figure 2, with more planets occurring in bins at small radius. But many of those small planets orbit relatively distant faint stars, and are not detected by TESS because their transits are not measured to the requisite S/N. For example, our default distributions produce 7857 transiting super Earths with radii between 2 and $3R_{\oplus}$. TESS's total for the 2–3 R_{\oplus} bin is 409 out of the 7857 due to incompleteness at the largest distances. (TESS is flux limited, and is not designed to be a volume-limited survey.) The total yield of super Earths from an all-sky transit survey is extremely sensitive to the light grasp and photometric precision of the survey, to a greater extent than uncertainties involving the super-Earth orbital size distribution. For gas-giant planets, S/N is not a limiting factor. Instead, the number of transiting giant planets detected is sensitive to their orbital architecture, and to galactic structure.

Finally, we evaluated the effect of visual versus IR brightness for M dwarfs. Our default simulation of TESS finds 320 super Earths within 35 pc of the Sun, regardless of their star's visual magnitude. If we strictly require V < 13.5 on the grounds that radial velocity confirmation would have to be done in the visible spectral range, then the number of TESS super Earths within 35 pc drops to 90. This implies that TESS is efficient for M dwarf transits due to its bandpass extending to 1000 nm. It also implies that successful development of precision IR radial velocity techniques may significantly increase the number of confirmed super Earths from a transit survey of bright stars.

3.4. Completeness of TESS for Nearby Transiting Habitable Super Earths

The potential discovery of habitable super Earths from the TESS survey is of special interest. We calculated the completeness of TESS for super Earths $(1-3R_{\oplus})$ by running our Monte Carlo simulation 500 times, and tabulating the fraction of habitable super Earths that TESS finds versus stellar mass and distance. The top panel of Figure 3 shows the completeness of TESS for transiting habitable super Earths versus stellar spectral type, in a volume out to 35 pc. All of the habitable super Earths found by TESS orbit M dwarfs. The completeness of TESS for $M > 0.5 M_{\odot}$ drops steeply because the habitable zone moves to longer orbital periods, where TESS does not sample two transits. Although TESS misses habitable super Earths orbiting stars more massive than about $0.5M_{\odot}$, it efficiently finds the transiting habitable super Earths nearest to our Sun. The completeness of TESS versus distance, including stars of all spectral types, is shown in the lower panel of Figure 3. TESS completeness is 93% at 10 pc, 80% at 20 pc, and 62% at 35 pc. It falls steeply at greater distances. The high completeness at near distances is



FIG. 3.—*Upper panel:* Completeness of the TESS survey for the detection of transiting super Earths $(1-3R\oplus)$ orbiting main-sequence stars of different masses, in a volume out to 35 pc distance. *Lower panel:* Completeness of the TESS survey for the detection of transiting super Earths orbiting in the habitable zone of stars of all spectral types, vs. distance.

consistent with the fact that the nearest stars are predominantly M dwarfs. TESS misses the few transiting habitable super Earths that orbit stars more massive than about $0.5M_{\odot}$. These misses are few in number because such stars have lower space densities than M dwarfs, and planets in their habitable zones have lower probabilities to transit compared to M dwarf habitable planets.

4. OVERVIEW OF SUPER-EARTH CHARACTERIZATION VIA TRANSITS

The characterization of transiting exoplanets relies primarily on observations at transit (planet partially eclipsing star) as well as secondary eclipse (star eclipsing planet). Besides the mass and radius determined from transit photometry (e.g., Charbonneau et al. 2006; Winn et al. 2008), the atmosphere can be characterized via its transmission spectrum during transit (Charbonneau et al. 2002; Redfield et al. 2008; Tinetti et al. 2007; Swain et al. 2008) and the emergent atmospheric spectrum can be measured using photometry and spectroscopy at secondary eclipse (Charbonneau et al. 2005, 2008; Deming et al. 2005, 2006, 2007; Knutson et al. 2008; Richardson et al. 2007; Grillmair et al. 2007, 2008). To estimate the sensitivity limits for these techniques as applied to super Earths, it is useful to first consider a simple characterization model. In this initial model, we assume that both the planet and star radiate as blackbodies. Some exoplanet atmospheric models predict that the atmospheric annulus of a transiting exoplanet will be opaque in the strongest lines over a height range of $\sim 5H$ (Seager & Sasselov 2002; Miller-Ricci et al. 2009), where H is the pressure scale height. Hence we approximate the magnitude of transit absorption, relative to a transparent continuum, as being equal to the area of an annulus of height = 5H. If the atmosphere is opaque over fewer scale heights, then the S/N in this simple model would be reduced in direct proportion. We calculate H using a temperature of 323 K, and a mean molecular weight of 22. These parameters are in an intermediate range for super Earths: the temperature is midway between the freezing and boiling points of water, and the atmospheric mean molecular weight is intermediate between free-hydrogen-rich and free-hydrogen-depleted (e.g., pure carbon dioxide) atmospheres (Miller-Ricci et al. 2009). Both this initial calculation, as well as our more detailed simulations (§§ 5 and 6), adopt cloud-free atmospheres. We here use a super-Earth mass of $10M_{\oplus}$, and a "dirty ocean planet" bulk composition, intermediate between rocky and icy. Using the mass-radius relations given by Seager et al. (2007) yields a planet radius of $2.3R_{\oplus}$. The depth of secondary eclipse is approximated as the planetto-star area ratio, times the ratio of Planck functions.

In analogy with Hubble Deep Field investigations (Gilliland et al. 1999), JWST characterization of a habitable super Earth would justify a large allocation of observing time, covering many transits and eclipses. We here adopt a total observation time of 200 hr. Calculation of S/N for each transit and eclipse observation requires accounting for the uncertainty of the outof-transit (or eclipse) baseline flux level. However, for the most interesting cases (i.e., habitable planets) the orbit periods are relatively long compared to hotter planets. Habitable planet observations will be limited by the number of transits that are visible to JWST within its 5 yr mission, not limited primarily by total observing time in hours. We therefore calculate the S/N using the condition that the 200 hr total applies only to the intransit/eclipse period, and that additional time will be available to measure baselines to a precision that does not significantly increase the error of the results.

Since we are here concerned with relatively nearby stars observed with a large-aperture space telescope, the observations are in the high-flux limit and we expect the dominant random noise source to be the photon noise of the host star and thermal background radiation, and we include these noise sources for this zeroth order model in the same detail as for our full MIRI and NIRSpec noise models (§§ 5 and 6). We adopt a telescope collecting area of 25 m^2 , and an end-to-end efficiency

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(electrons out/photons in) of 0.3 (typical for *Spitzer* and expected for *JWST*).

Figure 4 shows the results from this zeroth order calculation, as contours of constant S/N versus the distance to the system and the temperature (hence, mass and radius) of the host star. Transmission spectroscopy is more favorable at shorter wavelengths, because the transmission signal is proportional to the intensity of the stellar disk. We used water absorption at 2 μ m for the top panel of Figure 4. We summed the FWHM of several strong bands in model transmission spectra (Miller-Ricci et al. 2009) as an estimate of the number of wavelength points (160) that would be optically thick over 5*H* in height. This signal is detectable to S/N ~ 10 for systems out to ~12 pc, for a wide range of stellar temperatures. Moreover, the S/N contours bulge outward to higher S/N for the lower main sequence,



FIG. 4.—Upper panel: Contours of signal-to-noise ratio (S/N) for an intermediate composition $10M_{\oplus}$ habitable super Earth ($R = 2.3R_{\oplus}$, T = 323 K) observed during transit by a large-aperture space telescope (area 25 m^2), observing water absorption at 2 μ m, using a spectral resolving power of 1000, and summing the S/N over the 160 most optically thick wavelengths. *Lower panel:* S/N contours for the secondary eclipse of the same habitable super Earth, observed in thermal continuum radiation using a large-aperture cryogenic space telescope at 15 μ m, with a 3 μ m optical bandwidth (FWHM). Both panels assume the average of multiple transits or eclipses observed during a 200 hr program. The *overplotted points* show the TESS-discovered planets from our simulation, choosing all planets having radii $R = 2.3 \pm 1.0R_{\oplus}$, and $T = 323 \pm 50$ K.

showing the "small-star effect" (Charbonneau & Deming 2007). The lower panel of Figure 4 gives the S/N for secondary eclipse photometry at 15 μ m, near the peak of the planet's thermal emission. Detection of the secondary eclipse to S/N ~ 10 requires a distance closer than 10 pc for hotter stars, but the small-star effect extends from S/N ~ 10 to ~30 pc for cooler stars like M dwarfs.

Figure 5 shows the results from our zeroth order model in the case where we raise the planet's temperature to T = 500 K, increase the mass to $20M_{\oplus}$, and lower the mean molecular weight of the atmosphere to 2.3 (hydrogen-helium composition, with oxygen at solar abundance). This planet is a "hot super Earth," and the S/N for its characterization is considerably more favorable than for habitable super Earths.

We have overplotted some examples of TESS planets on Figure 4, extracting those planets that closely bracket the parameters assumed in generating the S/N contours. For Figure 4, we overplot the TESS planets having $R = 2.3 \pm 1.0 R_{\oplus}$, and $T = 323 \pm 50$ K, i.e., habitable super Earths. For Figure 4, TESS finds 5 habitable super Earths that could be characterized by NIRSpec to S/N ~ 10 or greater. A similar number of habitable super Earths could be characterized by MIRI secondary



FIG. 5.—Like Fig. 3, but using a planet of $20M_{\oplus}$, $R = 2.7R_{\oplus}$, hydrogenhelium–dominated atmospheric composition, and T = 500 K. The *overplotted points* are all TESS-discovered planets from our simulation, having $R = 2.7 \pm 1.0R_{\oplus}$, and $T = 500 \pm 50$ K.

eclipse photometry. For Figure 5, TESS finds many more hot ($T \ge 500$ K) super Earths, and we have overplotted examples of these. As we will see in later sections, these numbers are in reasonable agreement with much more exhaustive calculations.

5. SENSITIVITY AND NOISE MODELS FOR *JWST* INSTRUMENTS

JWST is well suited to transiting planet characterization (Clampin et al. 2009). It will orbit at the L2 Lagrangian point, where continuous observations will be possible without significant blocking by the Earth. The telescope will experience a favorable thermal environment, with low background emission. Engineering studies have defined the pixel response functions, and have developed a stringent error budget for pointing jitter. Moreover, *JWST* instruments will incorporate direct-to-digital detector readouts, with minimal suceptibility to electrical interference. We have utilized *JWST* Preliminary Design Review engineering estimates of telescope performance, to couple our TESS yield calculations to simulations of *JWST* super-Earth characterization.

Our simulations specify that *JWST* will observe all transits and eclipses of a given planet that are possible in principle during its 5 yr mission (Gardner et al. 2006; Clampin 2008). The rationale is that the maximum number can be objectively calculated, and readers can scale the S/N for smaller programs as they deem appropriate. The maximum number of transits/ eclipses is particularly large for the hotter planets, and scaling will show they can be observed to good S/N with far below the maximum number of transits.

Since the galactic coordinates of each Monte Carlo planetary system are tagged by our simulation, we transform to ecliptic coordinates and thereby calculate the time that each individual system is available in the *JWST* field of regard. We simulate each of the observable transits/eclipses, and we specifically include nonwhite noise sources during observations of each transit/eclipse. However, we expect that the aggegate S/N for observations of multiple events will be proportional to the square root of the number observed, because each event is a relative measurement (in-transit/eclipse compared to out-oftransit/eclipse), and the various transits/eclipses are independent. Hence our results can be adjusted to less complete observational programs by scaling the aggregate S/N in proportion to the inverse square root of the number of events that are actually observed.

In order to accurately evaluate the limits of characterization by *JWST*, we must construct a realistic noise model for the observations. In so doing, we draw on experience of *Spitzer* exoplanet programs, and current engineering error budgets and data for the *JWST* instruments, to simulate some effects that are foreseeable for each *JWST* instrument. We concentrate on two of the many possible modes of *JWST* observation, namely filter photometry at secondary eclipse using MIRI, and transmission spectroscopy at transit using NIRSpec.

5.1. MIRI

JWST's Mid-Infared Instrument (MIRI, Wright et al. 2004) will be the primary resource for exoplanet secondary eclipses, since it covers the 5–28 μ m wavelength range where secondary eclipse contrast is maximized. MIRI will provide filter imaging, low-resolution grism spectroscopy ($R \sim 100$), and medium-resolution spectroscopy ($R \sim 2000$). We have concentrated our noise model on imaging filter photometry, rather than MIRI spectroscopy, because we want to explore a photometric technique in addition to spectroscopic observations. This choice is conservative, because recording all wavelengths simultaneously could in principle give MIRI spectroscopy a factor of 2 improvement over photometric characterization.

Our MIRI noise model includes thermal background emission from the instrument, telescope, and sun shade, as calculated by Swinyard et al. (2004), as well as zodiacal thermal emission from our own solar system using the best available model (Kelsall et al. 1998) for the dependence on ecliptic latitude. We adopt a detector Fowler-8 read noise of 20 electrons pixel⁻¹, and we include 0.03 electrons s⁻¹ pixel⁻¹ dark current. We use a total reflectivity for the telescope optics of 0.88, and a transmittance of 0.52 for the MIRI instrument optics including the filters. The transmission curves of the MIRI filters are not yet available, but we include the requirement on their peak transmittance (>0.75) in the optics throughput, and we use square bandpass functions matching their required FWHM. We use detector quantum efficiencies of 0.5 and 0.6 at 11 and 15 μ m, respectively (Swinyard et al. 2004).

Our *JWST* noise model also includes an anticipated source of systematic error, based on *Spitzer* experience. The Si:As detectors that will be used in *JWST/*MIRI are similar to those in *Spitzer/*IRAC, and JWST will have pointing jitter like that of *Spitzer*, but projected to be of smaller amplitude. Hence, high-precision *Spitzer* photometry at 8 μ m provides our best current proxy for systematic errors in *JWST/*MIRI photometry.

Spitzer exhibits a periodic oscillation in pointing, with a 1 hr period and tens of milliarcsecond (mas) amplitude. This pointing error dithers the stellar image with respect to the detector pixels. Since the relative response of each pixel is imperfectly known (i.e., there are inaccuracies in the flat fielding), the pointing oscillation causes an intensity oscillation in aperture photometry. Assuming (conservatively) that the MIRI flat-fielding is not improved over *Spitzer*, we can use the *Spitzer* data to calculate the magnitude of this systematic error for MIRI photometry. This requires modeling some recent *Spitzer* data before turning our full attention to *JWST*/MIRI.

We developed a numerical model that simulates this effect. For the *Spitzer* data, we calculate the Fourier power spectrum of the Seager & Deming (2009) data, shown in Figure 6. This spectrum shows a peak at a period of slightly more than 1 hr, close to



FIG. 6.—Fourier power spectrum of a 33 hr sequence of *Spitzer* aperture photometry (Seager & Deming 2009), showing a peak (in *red*) due to a pointing oscillation in the telescope, with a period slightly longer than 1 hr. We use these data to estimate the pixel-to-pixel flat-fielding error for this mode of *Spitzer* observations, and then project this effect to *JWST* (see text).

the known period of the telescope oscillation. The power in this peak is 1.1% of the power integrated over all frequencies, hence the amplitude of the 1 hr oscillation in intensity at 8 μ m is $0.011^{1/2}\sigma = 0.105\sigma$, where σ is the standard deviation of the intensity time series. We know the amplitude of pointing oscillations at this frequency, from measuring the stellar image displacement in the Seager & Deming (2009) data. The link between pointing oscillation and intensity oscillation is the imperfect pixel-to-pixel flat-fielding. Hence we have sufficient data to determine the magnitude of pixel-to-pixel flat-fielding error for *Spitzer/IRAC*.

Our numerical model resamples *Spitzer's* 8 μ m PSF to 10 times finer spacing, and convolves it with a simulated detector grid, also resampled to 10 times finer spacing. We do the convolution at a series of pointing values, simulating the pointing oscillation in synthetic time-series photometry. The model includes flat-fielding errors on the scale of the actual IRAC pixels, with the error per pixel assigned from Gaussian random errors of a specified amplitude. We vary that amplitude until the standard deviation of the simulated time-series photometry matches the observed amplitude in intensity inferred from the Fourier analysis described above. On this basis, we estimate the IRAC flat-fielding error at 8 μ m to be 0.4%. We use that value in our MIRI noise model.

Our MIRI noise model adopts a point-spread function (PSF) from a ray-traced optical model of the telescope plus instrument,

for a central field location (Ronayette, S. 2009, private communication). This PSF is polychromatic, i.e., it is based on multiple wavelength samples over the 12.8 μ m filter bandpass. We spatially stretch it to represent the PSF at other wavelengths. The properties of the JWST pointing jitter can be anticipated from the engineering requirements (Ostazewski & Vermeer 2007). The telescope body pointing is controlled at a 16 Hz sampling rate, with a 0.02 Hz bandwidth. The fine guidance sensor is also sampled at 16 Hz, with a 0.6 Hz bandwidth. The 1σ amplitude of pointing jitter above the control bandwidth is 4.2 mas $axis^{-1}$, and within the bandwidth it is $5.1 \text{ mas axis}^{-1}$. Uncontrolled drift is specified to be less than 2.2 mas $axis^{-1}$ in a 10,000 s science exposure. We model the jitter within and above the control bandwidth as Gaussian random error of the specified magnitude, and we model the uncontrolled drift as monotonic and linear in time (worst case). This produces a 1σ deviation of 7 mas $axis^{-1}$ for a 10,000 s exposure. We note that exoplanet observers find a monotonic drift of much larger amplitude (~ hundreds of mas) in Spitzer pointing over ~ tens of hours.

We use these attitude control properties to generate pointing errors for a long time series of synthetic MIRI photometry. We adopt highly oversampled $(100\times)$ realizations of the MIRI detector grid and the PSF. The detector grid has 0.4% uncompensated response variation per original pixel. We shift the PSF relative to the detector grid, in accord with the synthetic pointing errors, multiply by the pixel sensitivities, and sum spatially to produce synthetic aperture photometry that contains only this error source. We model this error using a 10 s time resolution, but the actual exposure time for bright stars may be shorter than 10 s. Our noise model implicitly assumes that short exposures can be coadded (on the ground) to 10 s resolution, with no loss except for the increased overhead entailed by frequent detector reading (see § 5.2).

Noise from a representative 6 hr set of 10 s exposures is shown in Figure 7. We generated a 200 hr times series using this methodology, and we draw a sequential portion of that noise reservoir, starting at a random time, when modeling each eclipse for each planet. Figure 7 includes the histogram of modeled intensity fluctuations. This histogram is distinctly non-Gaussian, but the amplitude of this error source is generally small ($<10^{-4}$). Although *JWST* has a higher spatial resolving power than *Spitzer* (tending to increase this error), it also has much finer pixel scale, and much better telescope pointing control, which greatly reduces this source of photometry error.

Some planets will orbit bright stars, filling the MIRI detector in less than a 10 s exposure time. These systems require increased overhead to read-out the detector frequently in subarray mode. We calculate the exposure time required for each planethosting star to fill the brightest pixel to 10^5 electrons (Wright et al. 2004). Our noise model includes a 50 ms overhead per subarray read, and thereby accounts for the observing efficiency.



FIG. 7.—Upper panel: Intensity deviation in parts per million (ppm) for JWST/MIRI photometry at 15 μ m, from our MIRI noise model. These deviations are due to telescope pointing fluctuations and pixel-to-pixel errors in flat field-ing, based on *Spitzer* experience. *Lower panel:* Histogram of deviations from the upper panel, showing the non-Gaussian character of this noise source.

5.2. NIRSpec

The principal use of NIRSpec for transiting exoplanets will be to measure the transmission spectrum of their atmospheres during transit. We have modeled observations of transit water absorption in the 1.6 to 3 μ m region, and CO₂ absorption near 4.3 μ m, as observed using slit spectroscopy at a spectral resolving power R = 1000. The optical design of NIRSpec has been discussed by (Kohler et al. 2005). Our model adopts a total optical transmission for the NIRSpec optics after the slit of 0.4, and we also include the wavelength-dependent grating blaze function. As for optical losses at the entrance slit, we note the recent plan to include a $1.6^{"} \times 1.6^{"}$ entrance slit in NIRSpec, in specific response to the potential for exoplanet spectroscopy. No slit losses are included in our noise model because this large aperture will encompass virtually all of the energy in the telescope PSF.

Our noise model for NIRSpec includes the limitation on exposure time due to rapidly filling the detector wells (full well = 60,000 electrons). We use the Phoenix model atmospheres to calculate the time to achieve that signal level for the brightest pixel. As in the MIRI case, we model the systematic errors assuming a 10 s time resolution. Our model accounts for the number of times the detector must be read in a 10 s exposure, and we include the time to read a 16×4096 pixel subarray (0.85 s), since it reduces the observing time efficiency and increases the impact of read noise.

The noise properties of the NIRSpec detectors have been discussed by Rauscher et al. (2007). Our noise model for NIRSpec adopts a quantum efficiency of 0.8 for these HgCdTe detectors, independent of wavelength. We include detector read noise (6 electrons per Fowler-8) and dark current (0.03 e s^{-1}) in our model, but these sources of noise are not significant in comparison to source photon noise and systematic error due to intrapixel sensitivity variations. Recent measurements of the intrapixel sensitivity variations in these detectors (Hardya et al. 2008) show that the detector pixels have maximum response near pixel center, similar to the effect seen in the shortest wavelength channels of Spitzer/IRAC (Morales-Calderon et al. 2006). Figure 8 shows this intrapixel variation at a resolution of 0.1 pixel in each axis, as reconstructed by one of us (D. L.) based on engineering measurements at several locations in several pixels of the flight detectors. Our noise model synthesizes a large array of similar pixels, but we do not have complete information on possible pixel-to-pixel variation in the intrapixel curve. We therefore make the reasonable assumption that the average center-to-edge response variation is the same for all pixels, but that variations around a "smooth" intrapixel curve



FIG. 8.—Intrapixel sensitivity variation for a representative NIRSpec detector pixel, from engineering measurements of the flight detector. The upper traces show the average variation in the dispersion direction (*solid line*), and the spatial direction (*dashed line*). The lower traces divide the pixel into 10 strips parallel to the spectral dispersion, and they show the difference from a parabolic fit of response vs. distance from pixel center. The differences have been amplified by a factor of 4, and offset by 0.3, for clarity of presentation.

will differ from pixel to pixel. We fit a quadratic to our available center-to-edge data to define the smooth intrapixel curve (i.e., the average pixel). We measure the magnitude of deviations from this smooth curve, and we add Gaussian random noise having that standard deviation to the smooth curve, and thereby define the variations in the response curve of each modeled pixel, at a spatial resolution of 0.1 pixels in each axis.

Because there will be pointing jitter in the telescope, the spectrum will be dithered over the grid of detector pixels. This will result in an intensity variation at each wavelength, similar to the effect seen in Spitzer/IRAC photometry at 3.6 μ m and 4.5 μ m (Charbonneau et al. 2008). We model this process by using an optical model of the NIRSpec PSF at 2 μ m, and we scale the width of this PSF and convolve it at each wavelength with our synthetic pixel grid, using a spectrum of telescope pointing jitter and drift as described. The optical model of the spectrograph PSF uses the telescope PSF, and disperses it using a Gaussian kernel with a FWHM equal to the spectral resolution. We resample both the PSF and the detector pixel grid to 0.02 pixel resolution, for maximum precision. Dithering the resampled PSF over the resampled pixel grid gives a spectrum of non-Gaussian intensity error at each wavelength. We find that these fluctuations are highly correlated at different wavelengths, the magnitude and nature of the correlation depending on where each wavelength falls relative to the pixel grid. Since NIRSpec exoplanet observers will decorrelate these fluctuations, we perform that decorrelation in our simulations. Specifically, we take two wavelengths separated by one spectral resolution element (2 pixels), and we decorrelate intensity fluctuations at the first wavelength with respect to intensity fluctuations at the second wavelength. We thus use two fiducial wavelengths to construct a reservoir of intensity fluctuations that survive the decorrelation process. We call these "fundamental" fluctuations, and we draw from this reservoir when modeling other wavelengths, using a random selection process similar to our MIRI model. In real observations, observers will of course deal with this effect over all wavelengths simultaneously. Nevertheless, our procedure encapsulates the essence of the data analysis process that we envision, and it defines a core of fundamental fluctuations that will not be correctable in exoplanet observations. These fluctuations (not illustrated) have a magnitude and non-Gaussian distribution similar to the MIRI photometry fluctuations (Fig. 7).

6. TESS PLANETS AS OBSERVED BY JWST

We incorporate all of the specific parameters for each simulated TESS planet (impact parameter, temperature, orbital period, etc.) into the *JWST* instrument noise models, to predict the number of TESS planets of different types that *JWST* can characterize. As noted in § 5, we base the S/N values in this section on observing all possible transits/eclipses of each planet, within *JWST* viewing constraints.

6.1. MIRI Filter Photometry

Our values for the S/N of MIRI eclipse characterization are obtained by synthesizing time-series data, as described, for every observable eclipse of every TESS planet. These timeseries data contain all of the random error (source photon noise, thermal background, etc.) and systematic non-Gaussian errors as described in § 5.1. We solve for the depth of each eclipse, and we use the scatter in those derived eclipse depths to define the S/N for one eclipse. The aggregate S/N for all eclipses is the single eclipse S/N times the square root of the number of eclipses that are observed.

Although we have concentrated our MIRI simulations on secondary eclipses, we point out the significant potential for "around-the-orbit" observations (Knutson et al. 2007) applied to super Earths. A signal of small, or zero, amplitude in such observations can be used to establish that the planet has an atmosphere (Nutzman & Charbonneau 2008; Seager & Deming 2009), a fundamental inference. Note also that the sensitivity for around-the-orbit observations can in principle be higher than for an eclipse, because the full orbit affords more integration time.

In our eclipse simulations, we represent the super Earths' thermal emission using the model having intermediate content of free hydrogen by Miller-Ricci et al. (2009). For exo-Neptunes, we use a model by Miller-Ricci for GJ 436b. Temperature, rather than composition, has the dominant effect on MIRI filter photometry; hence we scale the thermal emission from each model as the temperature varies from planet to planet. This scaling adopts a blackbody continuum appropriate to the modeled temperature of each planet, but it does not change the fractional absorption. The latter approximation is particularly appropriate for MIRI, which would focus on the 15 μ m band of CO₂. The fractional absorption of this band is minimally sensitive to temperature because it is saturated and arises from the ground state. For the parent stars, we integrate Phoenix model atmosphere spectra over the filter bands to simulate the stellar signals.

Figure 9 shows a model spectrum of a super Earth in the 5 to 20 μ m spectral region, from Miller-Ricci et al. (2009), and marks the bandpasses of MIRI filters at 11.3 μ m and 15 μ m. Figure 10 shows the results of coupling the TESS simulations to our MIRI filter photometry noise model, for super Earths and exo-Neptunes. For super Earths we plot the S/N on the difference in contrast between the 11.3 μ m and 15 μ m bands, i.e., S/N on the absorption detection. For the exo-Neptunes, we plot the S/N in the 15 μ m band alone, but the S/N for Neptunes is sufficiently high to contemplate much higher spectral resolution results as well. S/N will scale down from Figure 10 as the square root of the number of eclipses. Neptune-sized planets will generally not require photometry of large numbers of eclipses in order to achieve good S/N. Figure 11 shows an example of simulated MIRI 15 μ m photometry for 10 eclipses of a warm exo-Neptune.



FIG. 9.—Relative flux vs. wavelength for a super-Earth model (Miller-Ricci et al. 2009). The *blue line* shows the blackbody continuum, and the *red brackets* denote the bandpasses of MIRI filters at 11.3 μ m and 15 μ m.

Eight habitable super Earths appear on Figure 10, but with lower S/N than for NIRSpec. This lower S/N arises in part from the background-limited nature of MIRI observations. The planet



FIG. 10.—S/N for TESS planets, measured by MIRI filter photometry at 15 μ m (the most favorable wavelength), vs. distance in parsecs. The S/N for super Earths applies to detection of the CO₂ absorption at 15 μ m relative to 11.3 μ m (see text). *Star symbols* are habitable super Earths, and *filled points* are super Earths having equilibrium temperatures above 373 K. *Open squares* are planets with radii between 3–5 Earth radii (Neptunes), at all temperatures, and their S/N is for detection of continuum radiation at 15 μ m. Points at the highest S/N tend to be hot planets in short-period orbits, lying at high ecliptic latitude where *JWST* has access to a very large number of eclipses.



FIG. 11.-Example of synthetic JWST/MIRI secondary eclipse photometry for a warm (T = 500 K) exo-Neptune, averaging 10 eclipses (120 hr total observing) as observed by JWST/MIRI at 15 μ m. The synthetic observations were binned to 1 minute time resolution. This planet has $R = 4R_{\oplus}$, and orbits at a =0.2 AU from a K2V star.

signal scales as the inverse square of the distance. However, as distance increases the noise approaches a constant level determined by the thermal background, hence $S/N \sim d^{-2}$. We will see in § 6.2 that NIRSpec characterization of habitable super Earths attains higher S/N on average, because the NIRSpec S/N is predominantly source photon-limited and hence $S/N \sim$ d^{-1} , not $\sim d^{-2}$. However, we expect the nearest habitable TESS super Earth to orbit a nearby $(d \lesssim 10 \text{ pc})$ late M dwarf, and MIRI will readily detect its secondary eclipse (Charbonneau & Deming 2007). We verified that the Charbonneau & Deming (2007) projections, as updated for their two cases by Charbonneau (2008), remain approximately consistent with our current MIRI noise model.

Many hotter super Earths are present in Figure 10 (filled circles), and their possible CO₂ absorption can be characterized by JWST to S/N ~10 or greater. Specifically, there are 446 super Earths above S/N = 10 in Figure 10. Although our simulation adopts exactly 1 planet star⁻¹, only 40% of our planets are super Earths, close to the super-Earth frequency claimed by Mayor et al. (2009). Adopting the Mayor et al. (2009) 30% frequency, TESS will discover ~330 hot super Earths whose CO₂ absorption can be measured by MIRI filter photometry. Above the radius of super Earths (>3 R_{\oplus} as defined by TESS), TESS will find many Neptune-size planets (up to $5R_{\oplus}$) whose eclipses can be measured by MIRI to high S/N (Fig. 11.)

6.2. NIRSpec Spectroscopy

We generate synthetic spectroscopy for a given synthetic planet by including the photon noise from the star, which can vary significantly with wavelength at the R = 1000 resolving power of NIRSpec, due to absorption features in the stellar spectra, especially for the M dwarfs. We use Phoenix model spectra to represent the stars, and we adopt planet models from Miller-





FIG. 12.—S/N for water absorption in TESS planets, measured by NIRSpec R = 1000 spectroscopy at 2 μ m, vs. distance in parsecs. The S/N is for the integral over wavelength from 1.7–3.0 μ m (see text). Solid circles are super Earths having equilibrium temperatures above 373 K. Star symbols are super Earths at habitable temperatures. Open squares are planets with radii between 3-5 Earth radii (Neptunes), at all temperatures. Unlike Figs. 3 and 4, we here invoke the condition that JWST observes all possible transits of a given system during its 5 yr mission. Points at the highest S/N tend to be hot planets in short-period orbits, lying at high ecliptic latitude where JWST has access to a very large number of transits.

Ricci et al. (2009), as described in the MIRI case. Since we are here dealing with transmission spectra, we scale the magnitude of the absorption from the fiducial planet model(s) in proportion to the calculated scale height of each planet's atmosphere, and



FIG. 13.—S/N for TESS planets in the 4.3 µm CO₂ band, measured by NIR-Spec R = 1000 spectroscopy, vs. distance in parsecs. The S/N is for the integral over wavelength from 4.0–4.6 μ m, i.e., the total S/N for the band. Solid circles are super Earths having equilibrium temperatures above 373 K, and star symbols are super Earths at habitable temperatures. Points at the highest S/N tend to be hot planets in short-period orbits, lying at high ecliptic latitude where JWST has access to a very large number of transits.



FIG. 14.—Upper panel: Points are synthetic NIRSpec observations of water absorption near 2 μ m, in a hot (T = 506 K) super Earth having $R = 2.1R_{\oplus}$, at a distance of 32 pc. The *red line* is the modeled spectrum, and the synthetic data have been binned in wavelength by a factor of 10, to a spectral resolving power R = 100, for clarity of presentation. The S/N for the aggregate detection of water absorption in this example is S/N = 163, for 301 hr. *Lower panel:* synthetic NIRSpec observations of water absorption in a habitable super Earth having T = 302 K and $R = 1.8R_{\oplus}$. The aggregate S/N for this detection is S/N = 16 for 122 hr, and the distance to this M dwarf planetary system is d = 20 pc.

the circumference of its atmospheric annulus. The spectra of the fiducial models have been calculated in full detail on a line-byline basis by Miller-Ricci et al. (2009). We preserve this spectrum shape, and scale the depth of the transmission spectrum in proportion to the projected area of the atmosphere. Note that the geometry of this problem causes an atmosphere to be opaque over a greater range of scale height for larger planets. We include a radius-dependent factor to account for this effect. Our synthetic time-series spectroscopy includes fundamental fluctuations due to the uncorrectable portion of the intrapixel effect, as described in § 5.2. For this purpose we use a large collection of synthetic 10 s exposures, and we draw a series of this non-Gaussian noise starting at a random time for each transit of each planet.

Computation of the S/N for each wavelength in the transit spectrum proceeds by constructing multiple transit curves at each wavelength, including synthetic photon noise and intrapixel fluctuations, and evaluating the S/N of the ensemble of transits as described for MIRI eclipses. The number of observable transits is taken to equal the number that can be observed for each planet by *JWST* during its 5 yr mission, under the constraint of *JWST*'s field of regard. Having evaluated the S/N at each wavelength, we also calculate a total S/N for the entire band, via a quadrature summation of the S/N values at each wavelength: $S/N_{band} = \sqrt{(\sum s/n_i^2)}$, where the sum is over the number of wavelength channels in the spectrum, and s/n_i is the S/N at a single wavelength *i*, averaged over all observed transits. When including the transmission signal in this calculation, we of course use only the variation in transmitted intensity versus wavelength, not the total absorption due to the entire planet. Figure 12 shows the results of this calculation (S/N_{band}) for water absorption near 2 μ m, and Figure 13 shows the corresponding result for detection of CO₂ absorption at 4.3 μ m.

Figure 14 shows an example of 2 μ m water absorption in both a hot and habitable super Earth, and Figure 15 shows examples of CO₂ absorption in similar planets.



FIG. 15.—Upper panel: synthetic NIRSpec observations (points) of carbon dioxide absorption near 4.3 μ m, in a hot (T = 797 K) super Earth having $R = 2.2R_{\oplus}$, at a distance of 18 pc, with the model overlaid (*red line*). The synthetic data have been binned in wavelength by a factor of 10, to a spectral resolving power R = 100, for clarity of presentation. The S/N for the aggregate detection of water absorption in this example is S/N = 150, observing for 480 hr in transit. (The S/N for 20 hr in transit would scale down to 31.) *Lower panel:* synthetic NIRSpec observations (points) of carbon dioxide absorption in a habitable super Earth having T = 308 K and $R = 2.3R_{\oplus}$, with the model spectrum overlaid (*blue line*). The aggregate S/N for this detection is S/N = 28 for 85 hr of in transit observing, and the distance to this planetary system is d = 22 pc.

7. DISCUSSION AND CONCLUSIONS

7.1. Our Results

Using our default distribution, i.e., that orbital sizes are distributed uniformly in log(a') (§ 3.1), places about 15% of our Monte Carlo planets within the HZ of their star. Thus, from Figure 1 (interpolating between the 0.1 and 0.3 curve), we project that the nearest transiting habitable planet will lie about 10 pc distant from our Sun. The nearest transiting habitable planet produced by our simulation lies at 9.5 pc from our Sun. Hence our simulation is consistent with the calculation presented in § 2. Moreover, as we show below, our sensitivity calculations are also internally consistent because our zeroth order results (§ 4) agree well with our more exhaustive calculations (§§ 5 and 6). We therefore discuss the prospects for habitable super-Earth discovery and characterization on the basis of our consistent, end-to-end simulation.

The above statements concerning nearby habitable planets are not restricted to super Earths, because our orbit distributions and radius distributions are independent. The architecture of our own solar system suggests that small planets should be associated with closer orbits, but we impose no such condition in our simulation. However, small planets outnumber large ones in our distributions, and the nearest transiting habitable planets we generate turn out to be super Earths, not Neptunes or Jupiters. Moreover, TESS finds these nearby habitable worlds very efficiently. Repeating our simulation 500 times, and considering only the super Earths, we tabulated the number of times that TESS finds at least one habitable super Earth closer than 35 pc. We adopted 0.3 super Earths star⁻¹ (Mayor et al. 2009), with our default distribution in orbital radius. The Mayor et al. (2009) estimate is a frequency: 30% of stars have at least one planet in the range up to Neptune-sized. The fact that Mayor et al. (2009) include Neptunes tends to make our 0.3 super Earths star⁻¹ value too high, but the fact that many stars will have multiple planets works in the opposite direction. Thus we believe that our 0.3 super Earths star⁻¹ value is reasonable, and it produces 0.047 super Earths star⁻¹ in the habitable zone. With this abundance, TESS finds at least one transiting habitable super Earth closer than 35 pc in 495 out of 500 simulations, a 99% probability.

Nearby habitable transiting super Earths can be characterized to a significant degree by *JWST*. The level of significance for this characterization is a function of astrophysical uncertainties, not primarily technological ones. For example, consider the situation for near-IR water absorption measured by transmission spectroscopy at transit. Our zeroth order calculation (Fig. 4) indicates that water absorption could be measured in 5 nearby habitable super Earths to S/N equal or exceeding 10, versus 8 from Figure 12. A key difference in these figures is that Figure 4 adopts a 200 hr program, whereas Figure 12 is based on observing all transits available within the *JWST* mission lifetime. But habitable planets tend to have longer orbit periods (compared to

"hot super Earths"), resulting in longer transits that occur less frequently. Inspecting the number of habitable super-Earth transits available to JWST per system, we find a natural dividing point near 60 transits. Five of the eight habitable super Earths in Figure 12 exhibit 60 or fewer transits, and the total in-transit time for each of them is less than 200 hr. These five habitable super Earths would be suitable to observe using a large JWST program. An example of synthetic JWST data for water absorption in a habitable super Earth with relatively low aggregate S/N $(S/N_{band} = 16)$ is shown in the lower panel of Figure 14. Super Earths represent about 40% of the planets in our simulation, close to the 30% frequency claimed by Mayor et al. (2009). (Hence, our simulations can be scaled to the Mayor et al. 2009 frequency by multiplying the number of super Earths by 0.75.) If their frequency is lower than Mayor et al. (2009) claim, then the number available for JWST characterization will be reduced in proportion.

Another source of astrophysical uncertainty regarding JWST characterization is the nature of the super-Earth atmosphere. We have used the intermediate case of Miller-Ricci et al. (2009), where the atmosphere is mildly reducing and inflated in height by the presence of residual hydrogen (either primordial, or outgassed). In the absence of this hydrogen, the mean molecular weight increases, the scale height decreases, and the water abundance also decreases. In that case, the S/N for transmission spectroscopy drops by a factor of ~ 3 , but JWST characterization remains possible for the closest super Earths. Specifically, five habitable super Earths would remain above $\mathrm{S/N}_{\mathrm{band}}=10,$ of which about three could be observed in 60 or fewer transits. If the frequency of super Earths is as low as 0.1 star^{-1} , and their atmospheres are hydrogen-depleted, then the number capable of being characterized in water absorption by JWST is expected to be one. On the other hand, if the frequency estimate of Mayor et al. (2009) is correct, and also their atmospheres are mildly reducing (10% hydrogen), then the expectation for the number that JWST can characterize via water absorption is five.

The situation for detection of CO₂ in absorption at 4.3 μ m during transit is similar to that of water. Figure 13 indicates seven habitable super Earths which could be observed to S/N \geq 10, of which four can be observed in fewer than 60 transits. Synthetic data for one example are shown in the lower panel of Figure 15. This habitable super Earth has S/N_{band} = 28, obtained by observing 58 transits. If the atmospheres of these worlds are hydrogen depleted, then the S/N drops by a factor of 2, and the number remaining above S/N = 10 in 60 transits or less drops to two. Factoring in possible variation in super-Earth frequency (as above), then our expectation for the number capable of being characterized in CO₂ absorption by *JWST* to S/N = 10 ranges from *one* to *five*.

The lower panel of Figure 4 indicates four habitable super Earths detected in thermal continuum radiation at secondary eclipse to S/N \geq 10. Simulations of CO₂ absorption observation using MIRI photometry at 15 μ m (Fig. 10) indicate one super Earth having $S/N \ge 10$, with an additional one at S/N = 8. These smaller numbers are consistent with the more demanding measurement of absorption versus a simple continuum brightness temperature measurement. An additional three super Earths are present in Figure 10 with $S/N \gtrsim 4$, sufficient to establish at least the presence of CO_2 absorption. Unlike the case of transit spectroscopy, this secondary eclipse technique is not sensitive to the scale height of the atmosphere, only to the total column density of absorbing molecules. Therefore we need only consider the frequency of super Earths. On this basis we expect the number capable of being characterized via a thermal continuum temperature measurement, and identification of CO_2 absorption, is from *one* to *four*.

Although our projections as quoted here are from a single Monte Carlo simulation of the TESS yield, we have rerun our simulations multiple times to verify the stability of the results in a statistical sense. We emphasize that *JWST* characterization of habitable worlds will require a large program, with priority given to the available transits/eclipses. Also, difficult choices will be necessary since each transit is precious but can be observed in only one mode (instrument, grating setting, etc.) at a time. Although the number of habitable planets capable of being characterized by *JWST* will be small, large numbers of warm to hot super Earths and exo-Neptunes will be readily characterized by *JWST*, and their aggregate properties will shed considerable light on the nature of icy and rocky planets in the solar neighborhood.

7.2. Comparison to Other Results

Pioneering work by Valenti et al. (2006) considered the possibility of *JWST/*NIRSpec characterization of habitable terrestrial planets that may transit nearby M dwarfs, based on models by Ehrehreich et al. (1999). They find that a habitable ocean planet orbiting an M3V star at 13 pc distance (J - magnitude = 8) can be well characterized using NIRSpec transmission spectroscopy. However, they find that water and CO₂ absorption in an Earth-sized planet with a high molecular weight atmosphere, i.e., a true Earth analog, can be detected only if the planet orbits an unrealistically bright and nearby M dwarf (J = 5, lying at 3 pc distance). Our calculations specifically include realistic details such as the number of transits available within the *JWST* field of regard, effects of noncentral

transits, systematic errors in the instrument, etc. However, we find that inclusion of these realistic factors does not greatly degrade the *JWST* sensitivity, and we concur with the Valenti et al. (2006) results. Specifically, we note that none of the habitable planets above S/N = 10 in Figure 12 are true Earth analogs, but this does not diminish their importance. All of them have radii exceeding $1.8R_{\oplus}$, and most of them are ocean planets.

Recently, Kaltenegger & Traub (2009) have calculated the detectability of Earth's transmission spectrum, illuminated by lower main sequence stars at 10 pc. They find that the transmission spectrum of our Earth has S/N < 1 for every molecular band in a single transit. However, many of the molecular features they tabulate would be observed to S/N > 10 in a 200 hr program (their Table 3).

Regardless of the situation for a true Earth analog, results for Earth cannot be easily extrapolated to super Earths. The atmospheric scale height is proportional to 1/g, where g is surface gravity. If we make the reasonable assumption that mass density is constant as radius varies, then $g \sim M/R_p^2 \sim R_p$. The projection of an atmospheric annulus of a given scale height is then proportional to R_p/g , and thus absorption seems independent of R_p . However, super Earths include ocean planets having lower mass densities (Seager et al. 2007; Fortney et al. 2007), which invalidates the assumption of constant density. Also, slant-path absorption does not scale strictly with H as R_p increases. In the slant-path geometry, for a given line opacity (cm² g⁻¹), the atmosphere is opaque over more scale heights as R_p increases. This modest but significant factor is included in our calculations.

We reiterate our conclusion that, depending on the frequency of occurrence of super Earths and the nature of their atmospheres, *JWST* will be able to measure the temperature, and detect molecular absorption bands, in one to four habitable TESS super Earths.

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